

$$1. \tan \theta = -\sqrt{3} \quad \left[\frac{\pi}{2}, \frac{5\pi}{2} \right]$$

$$\boxed{\frac{2\pi}{3}, \frac{5\pi}{3}}$$

$$2. 2 \sin(\theta + 47^\circ) = 1 \quad [0^\circ, 270^\circ]$$

$$\sin(\theta + 47^\circ) = \frac{1}{2}$$

$$\theta + 47^\circ = \sin^{-1} \frac{1}{2}$$

$$\theta + 47^\circ = 30^\circ, 150^\circ, 390^\circ$$

$$-47^\circ \quad -47^\circ \quad -47^\circ$$

$$\cancel{-17^\circ} \quad \boxed{103^\circ} \quad \cancel{357^\circ}$$

$$3. 4 \cos^2 \theta = 1$$

$$\sqrt{\cos^2 \theta} = \sqrt{\frac{1}{4}} \quad \left[-\frac{\pi}{2}, \frac{\pi}{2} \right]$$

$$\cos \theta = \pm \frac{1}{2}$$

$$\boxed{\frac{\pi}{3}, -\frac{\pi}{3}}$$

$$4. 2 \sin \theta \cos \theta = \sqrt{2} \cos \theta \quad [-\pi, 2\pi]$$

$$2 \sin \theta \cos \theta - \sqrt{2} \cos \theta = 0$$

$$\cos \theta (2 \sin \theta - \sqrt{2}) = 0$$

$$\cos \theta = 0 \quad 2 \sin \theta - \sqrt{2} = 0$$

$$\boxed{-\frac{\pi}{2}, \frac{\pi}{2}, \frac{3\pi}{2}}$$

$$\sin \theta = \frac{\sqrt{2}}{2}$$

$$\boxed{\frac{\pi}{4}, \frac{3\pi}{4}}$$